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Lecture notes - 17

BCA I year (II Sem)

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Subject - Mathematics - II

Topic - Plane - (Unit - 5)

Exp-20

Find the equation of plane through $(1, 2, 3)$, parallel to the plane $3x + 4y - 5z = 0$

Solution

Let the equation of plane parallel to the given plane $3x + 4y - 5z = 0$ is

$$3x + 4y - 5z = k$$

If it passes through $(1, 2, 3)$ then

$$3(1) + 4(2) - 5(3) = k$$

$$\Rightarrow k = -4$$

Then the required equation of plane is

$$3x + 4y - 5z = -4$$

$$\text{or } 3x + 4y - 5z + 4 = 0$$

Exp-21

Find the equation of plane through $(-1, 1, 1)$ and $(1, -1, 1)$ and perpendicular to the plane $x + 2y + 2z = 5$

Solution

Let the equation of plane is

$$Ax + By + Cz + D = 0 \quad \text{--- (i)}$$

If it passes through $(-1, 1, 1)$ and $(1, -1, 1)$

Then $\Pi - -A + B + C + D = 0$ ——— (ii)
 and $A - B + C + D = 0$ ——— (iii)

Given, Equation (i) is perpendicular to the plane $x + 2y + 2z = 5$

So $A + 2B + 2C = 0$ ——— (iv)

(By the Condition of perpendicularity)

From (ii) & (iii) $A - B = 0, C = 0$ ——— (v)

From (iv) and (v)

$$\frac{A}{-2-0} = \frac{B}{0-2} = \frac{C}{2-(-1)} = \lambda$$

$$\Rightarrow \frac{A}{-2} = \frac{B}{-2} = \frac{C}{3} = \lambda$$

$$\Rightarrow A = -2\lambda, B = -2\lambda, C = 3\lambda$$

Put in Eqn (i), From (ii) $D = 3$

$$-2x - 2y + 3z - 3 = 0$$

Which is equation of required plane.

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Solve itself

Ques-1 Find the equation of the plane through $(1, 0, -2)$ and perpendicular to each of the plane $2x + y - z = +2$ and $x - y - z - 3 = 0$

Solution Same as Exp-21

Exp-24 A variable plane passes through a fixed point (α, β, γ) and meets the axes of at A, B, C . Show that the locus of the point of intersection of the planes through A, B, C to the Co-ordinate plane is $\alpha x^{-1} + \beta y^{-1} + \gamma z^{-1} = 1$

Solution Let the equation of the variable plane is $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ ——— ①

Where a, b, c are parameter.

\therefore The plane ① passes through the point (α, β, γ)
 $\Rightarrow \frac{\alpha}{a} + \frac{\beta}{b} + \frac{\gamma}{c} = 1$ ——— ②

The plane ① meets the Co-ordinate axes in the point A, B, C whose Co-ordinates are $(a, 0, 0)$ $(0, b, 0)$ $(0, 0, c)$. The equation of plane through A, B, C and parallel to the Co-ordinate axes are $x = a$, $y = b$, $z = c$ respectively.

Then from ②

$$\frac{\alpha}{a} + \frac{\beta}{b} + \frac{\gamma}{c} = 1$$

$$\text{OR } \alpha x^{-1} + \beta y^{-1} + \gamma z^{-1} = 1 \quad \text{Proved}$$