## Digital Circuits - Conversion of Flip-Flops

In previous chapter, we discussed the four flip-flops, namely SR flip-flop, D flip-flop, JK flip-flop \& T flipflop. We can convert one flip-flop into the remaining three flip-flops by including some additional logic. So, there will be total of twelve flip-flop conversions.

Follow these steps for converting one flip-flop to the other.

- Consider the characteristic table of desired flip-flop.
- Fill the excitation values inputs of given flip-flop for each combination of present state and next state. The excitation table for all flip-flops is shown below.

| Present State | Next State | SR flip-flop inputs |  | D flip-flop input | JK flip-flop inputs | T flip-flop input |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{Q} t$ | Q $t+1$ | $\mathbf{S}$ | $\mathbf{R}$ | $\mathbf{D}$ | $\mathbf{J}$ | $\mathbf{K}$ | $\mathbf{T}$ |
| 0 | 0 | 0 | x | 0 |  |  |  |
| 0 | 1 | 1 | 0 | 1 | 1 | x | 0 |
| 1 | 0 | 0 | 1 | 0 | x | 1 | 1 |
| 1 | 1 | x | 0 | 1 | x | 0 | 1 |

- Get the simplified expressions for each excitation input. If necessary, use Kmaps for simplifying.
- Draw the circuit diagram of desired flip-flop according to the simplified expressions using given flip-flop and necessary logic gates.

Now, let us convert few flip-flops into other. Follow the same process for remaining flipflop conversions.

## SR Flip-Flop to other Flip-Flop Conversions

Following are the three possible conversions of SR flip-flop to other flip-flops.

- $\quad$ SR flip-flop to D flip-flop
- $\quad$ SR flip-flop to JK flip-flop
- $\quad$ SR flip-flop to $T$ flip-flop


## SR flip-flop to D flip-flop conversion

Here, the given flip-flop is SR flip-flop and the desired flip-flop is D flip-flop. Therefore, consider the following characteristic table of $D$ flip-flop.

| D flip-flop input | Present State | Next State |
| :---: | :---: | :---: |
| D | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

We know that SR flip-flop has two inputs S \& R. So, write down the excitation values of SR flip-flop for each combination of present state and next state values. The following table shows the characteristic table of $D$ flip-flop along with the excitation inputs of SR flip-flop.

| D flip-flop input | Present State | Next State |  | SR flip-flop inputs |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{D}$ | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ | $\mathbf{S}$ | $\mathbf{R}$ |  |
| 0 | 0 | 0 | 0 |  |  |
| 0 | 1 | 0 | 0 | 1 |  |
| 1 | 0 | 1 | 1 | 0 |  |
| 1 | 1 | 1 | $x$ | 0 |  |

From the above table, we can write the Boolean functions for each input as below.

$$
\begin{aligned}
& S=m_{2}+d_{3} \\
& R=m_{1}+d_{0}
\end{aligned}
$$

We can use 2 variable K-Maps for getting simplified expressions for these inputs. The k-Maps for $S \& R$ are shown below.


So, we got $S=D \& R=D^{\prime}$ after simplifying. The circuit diagram of $D$ flip-flop is shown in the following figure.


This circuit consists of SR flip-flop and an inverter. This inverter produces an output, which is complement of input, D . So, the overall circuit has single input, D and two outputs $\mathrm{Q} t \& \mathrm{Q} t$ '. Hence, it is a $\mathbf{D}$ flipflop. Similarly, you can do other two conversions.

## D Flip-Flop to other Flip-Flop Conversions

Following are the three possible conversions of $D$ flip-flop to other flip-flops.

- D flip-flop to T flip-flop
- D flip-flop to SR flip-flop
- D flip-flop to JK flip-flop


## D flip-flop to T flip-flop conversion

Here, the given flip-flop is D flip-flop and the desired flip-flop is T flip-flop. Therefore, consider the following characteristic table of T flip-flop.

| T flip-flop input | Present State | Next State |
| :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

We know that $D$ flip-flop has single input $D$. So, write down the excitation values of $D$ flip-flop for each combination of present state and next state values. The following table shows the characteristic table of T flip-flop along with the excitation input of $D$ flip-flop.

| T flip-flop input | Present State | Next State | D flip-flop input |
| :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ | $\mathbf{D}$ |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |

From the above table, we can directly write the Boolean function of $D$ as below.

$$
D=T \oplus Q(t)
$$

So, we require a two input Exclusive-OR gate along with $D$ flip-flop. The circuit diagram of $T$ flip-flop is shown in the following figure.


This circuit consists of $D$ flip-flop and an Exclusive-OR gate. This Exclusive-OR gate produces an output, which is Ex-OR of T and Q $t$. So, the overall circuit has single input, T and two outputs $\mathrm{Q} t \& \mathrm{Q} t$ '. Hence, it is a T flip-flop. Similarly, you can do other two conversions.

## JK Flip-Flop to other Flip-Flop Conversions

Following are the three possible conversions of JK flip-flop to other flip-flops.

- JK flip-flop to T flip-flop
- JK flip-flop to D flip-flop
- JK flip-flop to SR flip-flop


## JK flip-flop to T flip-flop conversion

Here, the given flip-flop is JK flip-flop and the desired flip-flop is T flip-flop. Therefore, consider the following characteristic table of T flip-flop.

| T flip-flop input | Present State | Next State |
| :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

We know that JK flip-flop has two inputs J \& K. So, write down the excitation values of JK flip-flop for each combination of present state and next state values. The following table shows the characteristic table of T
flip-flop along with the excitation inputs of JK flipflop.

| T flip-flop input | Present State | Next State | JK flip-flop inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ | $\mathbf{J}$ | $\mathbf{K}$ |
| 0 | 0 | 0 | 0 | x |
| 0 | 1 | 1 | x | 0 |
| 1 | 0 | 1 | 1 | x |
| 1 | 1 | 0 | x | 1 |

From the above table, we can write the Boolean functions for each input as below.

$$
\begin{aligned}
& J=m_{2}+d_{1}+d_{3} \\
& K=m_{3}+d_{0}+d_{2}
\end{aligned}
$$

We can use 2 variable K-Maps for getting simplified expressions for these two inputs. The k-Maps for J \& K are shown below.


K-Map for K


So, we got, $\mathrm{J}=\mathrm{T} \& \mathrm{~K}=\mathrm{T}$ after simplifying. The circuit diagram of T flip-flop is shown in the following figure.


This circuit consists of JK flip-flop only. It doesn't require any other gates. Just connect the same input T to both $\mathrm{J} \& \mathrm{~K}$. So, the overall circuit has single input, T and two outputs $\mathrm{Q} t \& \mathrm{Q} t$ '. Hence, it is a T flip-flop. Similarly, you can do other two conversions.

## T Flip-Flop to other Flip-Flop Conversions

Following are the three possible conversions of T flip-flop to other flip-flops.

- T flip-flop to D flip-flop
- T flip-flop to SR flip-flop
- T flip-flop to JK flip-flop


## T flip-flop to D flip-flop conversion

Here, the given flip-flop is T flip-flop and the desired flip-flop is D flip-flop. Therefore, consider the characteristic table of $D$ flip-flop and write down the excitation values of $T$ flip-flop for each combination of present state and next state values. The following table shows the characteristic table of $D$ flip-flop along with the excitation input of T flip-flop.

| D flip-flop input | Present State | Next State | T flip-flop input |
| :---: | :---: | :---: | :---: |
| D | $\mathbf{Q} t$ | $\mathbf{Q} t+1$ | $\mathbf{T}$ |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 |

From the above table, we can directly write the Boolean function of T as below.

$$
T=D \oplus Q(t)
$$

So, we require a two input Exclusive-OR gate along with $T$ flip-flop. The circuit diagram of $D$ flip-flop is shown in the following figure.


This circuit consists of $T$ flip-flop and an Exclusive-OR gate. This Exclusive-OR gate produces an output, which is Ex-OR of D and $\mathrm{Q} t$. So, the overall circuit has single input, D and two outputs $\mathrm{Q} t \& \mathrm{Q} t^{\prime}$. Hence, it is a D flip-flop. Similarly, you can do other two conversions.

